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Cultural artefacts as a metaphor to communicate mathematical ideas

Artefatos culturais como uma metáfora para comunicação de ideias matemáticas

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Abstract: The cultural artifacts created by the culture of a particular group of people embed sophisticated mathematical ideas and knowledge. The cultural artifacts familiar to students mediate to communicate abstract ideas of mathematics. This paper is intended to explore the mathematical ideas embedded in cultural artifacts and to assess its contribution to the process of teaching and learning of school mathematics. The ethnographic methodology was used to collect the data. Highly sophisticated mathematical ideas were found in the analysis of different cultural artifacts observed in the out-of-school environment. The cultural artifacts familiar to students are the source domain of conceptual metaphor to communicate difficult and abstract concepts of mathematics. Both teachers and students reported that the cultural artefacts and different cultural activities of the group of people help them in teaching and learning of mathematical concepts.

Keywords: Conceptual Metaphor. Cultural Artefacts. Ethnography. Ethnomathematics. Mathematical Ideas.

Los artefactos culturales como una metáfora para la comunicación de las ideas matemáticas

Resumen: Los artefactos culturales creados por la cultura de un grupo particular de personas incorporan ideas y conocimientos matemáticos sofisticados. Los artefactos culturales familiares para los estudiantes median para comunicar ideas abstractas de las matemáticas. Este documento tiene como objetivo explorar las ideas matemáticas incrustadas en artefactos culturales y evaluar su contribución al proceso de enseñanza y aprendizaje de las matemáticas escolares. La metodología etnográfica se utilizó para recopilar los datos. Se encontraron ideas matemáticas altamente sofisticadas en el análisis de diferentes artefactos culturales observados en el entorno fuera de la escuela. Los artefactos culturales familiares para los estudiantes son el dominio fuente de la metáfora conceptual para comunicar conceptos matemáticos difíciles y abstractos. Tanto maestros como estudiantes informaron que los artefactos culturales y las diferentes actividades culturales del grupo de personas los ayudan a enseñar y aprender conceptos matemáticos.

Palabras clave: Metáfora Conceptual. Artefactos Culturales. Etnografía. Etnomatemáticas. Ideas Matemáticas.

Artefatos culturais como uma metáfora para comunicação de ideias matemáticas

Resumo: Os artefatos culturais criados pela cultura de um determinado grupo de pessoas incorporam ideias e conhecimentos matemáticos sofisticados. Os artefatos culturais familiares aos alunos auxiliam na mediação para comunicar ideias abstratas da Matemática. Este artigo objetiva explorar as ideias matemáticas incorporadas aos artefatos culturais e avaliar sua contribuição para o processo de ensino e aprendizagem da matemática escolar. A metodologia etnográfica foi utilizada para a coleta dos dados. Ideias matemáticas altamente sofisticadas foram encontradas na análise de diferentes artefatos culturais observados no ambiente extra-escolar. Os artefatos culturais familiares aos alunos são o domínio de origem da metáfora conceitual para comunicar conceitos difíceis e abstratos da matemática. Professores e alunos relataram que os artefatos culturais e as diferentes atividades culturais do grupo de pessoas os ajudam a ensinar e aprender conceitos matemáticos.

Palavras-chave: Metáfora Conceitual, Artefatos Culturais, Etnografia, Etnomatemática, Ideias Matemáticas.

1 Understanding Conceptual Metaphor

Everyone does use metaphors in their day-to-day interactions with others. People may use metaphors even without noticing it. People understand some abstract and difficult concepts through the connection with familiar objects. The familiar concepts are based on their own experiences and cultural activities. Metaphor can facilitate to understand the abstract phenomena. Metaphor is a mapping between two conceptual domains which provides a powerful tool to understand one domain of knowledge in terms of another. The conceptual metaphors help to deal with relatively unfamiliar and abstract domains of experience in a familiar and tangible way. The set of known and familiar ideas helps to understand difficult and abstract concepts.

There are two parts of a conceptual metaphor: target domain and source domain. Basically, metaphor is a mapping between the source domain and the target domain. The source domain is familiar, concrete and based on everyday activities and experiences of learners whereas the target domain is an unknown, abstract and difficult set of ideas. Some common everyday conceptual metaphor includes "LIFE is a JOURNEY". Here, LIFE is the target domain as it holds unknown and abstract ideas whereas JOURNEY is the source domain because it is the class of concrete vehicles that help to understand the target. Some people may have a journey but may not have a destination. There may arise obstacles during the journey, sometimes may come joyful moments as well.

People may face ups and downs during their journey. JOURNEY helps to understand the term LIFE in terms of various familiar activities and experiences. In fact, metaphor is a mapping between two conceptual domains, which provides a powerful tool to understand the target domain of knowledge in terms of simple and familiar ideas. Metaphor simply means the representation of abstract entities through very simple, familiar and meaningful objects. It can be taken as a mapping that the abstract ideas map into concrete, strong and meaningful images that are developed in different social and cultural context for a different purpose.

English (1997) sees metaphors as a tool for creating formal concepts out of image

schemas, and of restructuring these concepts in complex ways. Lakoff and Nunez (2000) also argue that “the conceptual metaphor’s primary function is to allow us to reason about relatively abstract domains using the inferential structure of relatively concrete domains,” (p. 42) with structures of image schemas preserved by this mapping. Thus, metaphor can be considered as a mechanism for connecting two types of knowledge of which the new knowledge is comprehended through already existed familiar concepts.

Lakoff and Nunez (2000) created three types of conceptual metaphors and they are known as grounding metaphors, linking metaphors and extraneous metaphors. The grounding metaphors allow us to ground our understanding of mathematical ideas based on everyday experience. For instance, the abstract mathematical idea of addition as putting things into piles/bags or adding things to a collection, subtraction as taking things away from a collection, sets as containers, members of a set as objects in a container. In this regard, Danesi (2007) argued that thermometer, as students are familiar with this device, helps to conceptualize positive integer, negative integer and number zero. The negative integers are placed below the zero and positive integer is above zero in thermometers. Thus, the thermometer is a grounding metaphor to understand an abstract concept of integers.

The linking metaphors allow us to link one branch of mathematics to its other branches. For example, the metaphor “NUMBERS is a POINT ON A LINE” links arithmetic to geometry. Thus, the linking metaphors allow conceptualizing the ideas of arithmetic in terms of geometry. And the next is extraneous metaphors. Lakoff and Nunez (2000) affirm that “extraneous metaphor or metaphors that have nothing whatever to do with either the grounding of mathematics or the structure of mathematics itself. Unfortunately, the term metaphor when applied to mathematics has mostly referred to such extraneous metaphors” (p. 53). The staircase is an example of extraneous metaphor of the “step function” because when graphed the step function can look similar to a staircase. The image of staircase has nothing whatever to do with either the inherent content of the grounding of the mathematics, although the visual is a helpful reminder of how this function would look when graphed (LAKOFF & NUNEZ, 2000; BEARDEN, 2012).

Likewise, “FUNCTION is a MACHINE” is a metaphor. The source domain of this metaphor is MACHINE and the target domain is the mathematical concept of FUNCTIONS. Extraneous metaphors can be eliminated without any substantive change in the conceptual structure of mathematics, whereas eliminating grounding or linking metaphors would make much of the conceptual content of mathematics disappear. Fyhn (2007) maintained that “Some Sami mittens have the pattern grouse footprints on their edges. These repeating patterns show a connection

between embodied experiences and ornamentation. Ski trails, as well as animal footprints, perform patterns in the snow, patterns with different symmetry properties” (p. 246). The patterns in snow are concrete and familiar example of some geometrical ideas, which facilitates to understand abstract geometrical concepts.

And footprints in the snow are the source domain to understand the target domain, some properties of symmetry. In this paper, the metaphors are the tools whose source domains are the out-of-school mathematical ideas embedded in cultural artefacts, monuments, arts, language and literature, games, and their everyday activities and the school mathematics, the target domain. The use of cultural artifacts in mathematics classroom activities can be articulated in various stages of teaching and learning of content objectives. The use of some artifacts like bottle and labels, restaurant bill, electricity bill, the weather forecast presented in a newspaper, etc., enables the teacher to pose a great deal of possible questions, remarks, culturally and scientifically interesting inquiries in the process of instruction.

In this study, I take the term (cultural) metaphor as the material culture that can be mediated to the teaching and learning of school mathematics. It has educative significance and source of inspiration for the mathematical knowledge generation, transformation, distribution and diffusion to the students and teachers of mathematics. The ethnomathematical ideas embedded in cultural artefacts can serve as the most powerful metaphor in the process of teaching and learning of formal mathematics. In my study, cultural metaphors are tools, which connect students’ out-of-school environmental activities to understand school mathematics.

2 Cultural Artefacts and Ethnomathematics

Cultural artefacts are anything or object that is created by the culture of a particular group of people that helps to define their culture. Gueudet and Trouche (2009) extend the definition of artefact by introducing the term resources to encompass any artefact with the potential to promote the process of learning. There are different types of cultural artefacts, which reflect the cultural identity of different groups of people. Some of them are dress, house, utensil, basket, ornament, painting, design and so on. All these artefacts give the information about the culture of its creators and the ideas associated with these objects. Bonotto (2007) viewed that the extensive use of cultural artefacts makes school mathematics more meaningful. For him, the cultural artefacts introduced into mathematics classroom are concrete materials, which children typically meet in real-life situations. These concrete materials can be a suitable tool to transfer one domain of

knowledge to another. In this paper, I explored mathematical ideas embedded in cultural artefacts of different physical objects and its use as an instructional material that mediated the teaching and learning of school mathematics.

Bishop (1991) believes that mathematics is a cultural product, which has developed as a result of various activities, and that counting, locating, measuring, designing, playing, and explaining are all part of that cultural product. Everyday life is impregnated in the knowledge and practices of a culture. At all times, individuals are comparing, classifying, quantifying, measuring, explaining, inferring, generalizing, and evaluating, using the material and intellectual instruments that belong to their culture (D'AMBROSIO, 2006). The cultural activities of human beings invented some kind of mathematical knowledge and concepts. Every culture has developed mathematics practices consistent with their needs and interest in everyday activities. Naturally, it is not surprising that extremely practical concepts such as numbers and counting have arisen in all cultures.

There is a lack of evidence and the exact date that the people of the world started to weave the items. For thousands of years, people have been weaving baskets, hats, mats and other items. Different cultures have carried out weaving using different materials like grass, leaves, clothes, feathers, paper and other local materials. An artefact may be considered as any human creation and it has different purposes for different peoples. The cultural artefacts are potentially a very powerful metaphor to communicate abstract mathematical ideas. For example, CIRCLE is a BANGLE is an extraneous metaphor in which abstract concept of CIRCLE can be understood with the help of known and familiar artefacts, the BANGLE. On the same note, the money of different denominations has some sort of purpose for some community members but in an educational context to be used as a metaphor for teaching and learning of different concepts of mathematics. In this study, I have collected some cultural artefacts that have potentially very powerful teaching and learning tool to communicate abstract mathematical ideas.

Ethnomathematics may be described as the study of mathematical ideas and activities as embedded in their cultural context. Further D' Ambrosio (2006) defined ethnomathematics as "the mathematics which is practiced among identifiable cultural groups such as national-tribe societies, labor groups, children of certain age brackets and professional classes and so on" (p. 44). Ethnomathematics can be described as the way people from a particular culture have common systems for dealing with quantitative, relational, and spatial aspects of their lives (BARTON, 1996). It follows what Knijnik (1997) cited by Alanguí (2017) describes as an ethnomathematical approach, one that is characterized by the investigation of the traditions, practices, and mathematical concepts of a subordinated social group and the pedagogical work, which was developed in order

for the group to be able to interpret and decode its knowledge.

The ethnomathematical ideas of the group of people have generally been excluded from discussions of formal and academic mathematics. Rosa and Gavarrete (2017) also viewed that their mathematical knowledge and learning approaches are not taken into consideration in the formal school mathematics curricula. The mathematical ideas from the group of working-class people culture, the acknowledgment of their ways of knowledge generation and transmission, and students' experiences should be blended with formal mathematics in the classrooms (PRADHAN, 2017). In attempting to create and integrate mathematical materials related to different cultures and that draw on students' own experiences in an instructional mathematics curriculum, it is possible to apply ethnomathematical strategies in teaching and learning mathematics (ROSA & GAVARRETE, 2017).

Pradhan (2012) did a study to explore the knowledge generation of Chundara and to compare and contrast the ways that they learn and teach in their everyday activities from the school pedagogy. The main finding of the study was that Chundaras teaching and learning activity involved participatory and cooperative approaches in which they learn with the help of their parents as Vygotsky (1978) seeing learning as an activity in which shared mathematical meanings are constructed socially. However, they are using implicit mathematical knowledge in their everyday activities and the construction of these wooden stuffs. Millroy (1992) found that the group of carpenters used the concept of tacit knowledge of mathematical ideas. This concept of tacit knowledge implies that most people know more than they can tell. Tacit knowledge manifests itself through human activities and is not necessarily expressed or expressible in written or spoken form. Such knowledge helps them to develop mathematical ideas and thinking in those groups of people. The group of people in the out-of-school context have been developing their own mathematical ideas and knowledge and practicing for long to sustain their lives.

The studies reveal that all cultures have basic counting, sorting and deciphering methods and that these have arisen independently in different places around the world. It is important to connect the out-of-school mathematical ideas for the understanding of the abstract concept of mathematics. The familiar concepts of students based on their culture, everyday activities and experiences would be the source to understand the target that is relatively abstract, difficult and unfamiliar to them. As metaphor is a mapping between two conceptual domain, the ethnomathematical ideas, concepts embedded in different cultural artefacts, and associated practices are the source domain which mediates to understand difficult and abstract concepts of school mathematics. Thus, ethnomathematical ideas embedded in cultural artefacts help to

conceptualize abstract mathematical ideas by connecting children's everyday activities. In this paper, I argued that the cultural artefacts and embedded ethnomathematical ideas and concepts facilitate the understanding of school mathematics.

3 Research Questions

The main objective of this study was to explore the ethnomathematical ideas embedded in different cultural artefacts and analyze its contribution to the teaching and learning of mathematics. In order to achieve this objective, I formulated the following research questions:

- What mathematical ideas embed in cultural artifacts?
- How do cultural artifacts facilitate teaching and learning of school mathematics?

4 Conceptual Framework

The framework developed in this study shows how the cultural artefacts and ethnomathematical ideas of different groups of people can be a mediated tool for the teaching and learning of school mathematics. It is assumed that students' familiar contexts become a powerful source in mathematics teaching and learning. Connecting students' out-of-school mathematical ideas to teaching school mathematics is really a great problem for the teachers. Regarding the incorporation of cultural knowledge in classroom teaching, Paulo Freire (1970) suggested that "children's cultural capital — the knowledge children bring to school from their home and cultural environment — should be welcomed and utilized in school for teaching and knowledge building purposes" (as cited in STRINGER, CHRISTENSEN & BALDWIN, 2010, p. 24). In this way, students' out-of-school knowledge that is embedded in their culture of the community is celebrated and utilized as a source domain of the conceptual metaphor in an appropriate way in the classroom teaching and learning process. The mathematical ideas embedded in the cultural artefacts from the out-of-school environment of the learners' community was observed and incorporated in the process of teaching and learning of school mathematics.

The mathematical understanding is important for everyone and they are using mathematical ideas and knowledge to perform everyday work. The mathematical knowledge and ideas are implicitly used in out-of-school culture. My argument in this study is that cultural artefacts and the ethnomathematical ideas embedded in different cultural activities mediate to the understanding of school mathematics. This framework is based on the theory of conceptual

metaphor that indicates the connection between the source domain and the target domain for meaningful mathematics teaching and learning. The source domain is the cultural artefacts and the associated practices, which are always familiar, known, and concrete to the learners. The knowledge to be learnt is the target domain, which is considered as abstract and difficult. The framework speaks that the incorporation of ethnomathematical ideas, embedded in the cultural artefacts, in the classroom teaching can facilitate the understanding of school mathematics. The connections of these concepts and ideas in the teaching and learning can enhance school mathematics.

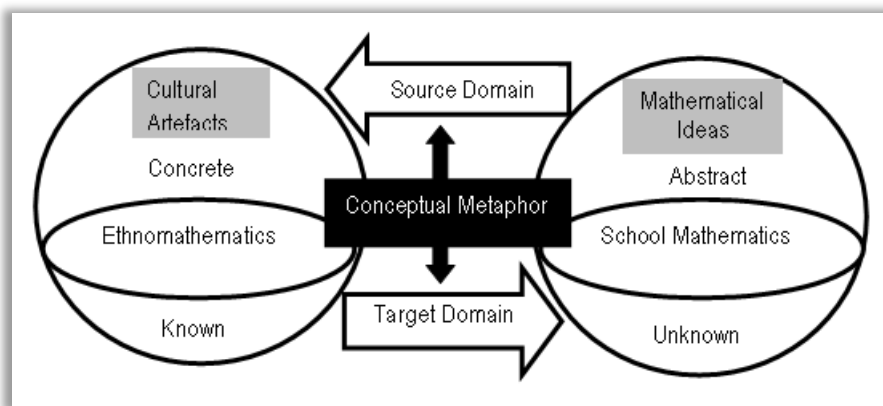


Figure 1: Connecting cultural artifacts and school mathematics (Author's personal file)

The learners' culture and everyday activities regarding ethnomathematical ideas are an integral part of education in general and learning mathematics in particular. This framework highlighted the integration of the mathematical concepts which are practiced in the learner's culture with those of school mathematics (ADAM, 2004; ALANGUI, 2017). It is believed that classrooms and other learning environments cannot be isolated from the communities in which they are embedded, and students come to school bringing with them values, norms, and concepts they have acquired from their culture and environment. The students' home culture and ethnomathematical ideas provide opportunities to connect to school mathematics. Figure 1 depicts a conceptual framework to connect the students' out-of-school knowledge, embedded mathematical ideas in their cultural activities to school mathematics. This framework allows for a wider set of cultural artefacts has the possibility in the discussion of formal mathematical ideas. This suggests that it is possible to connect school mathematics through the ethnomathematical ideas and the out-of-school context of the learners.

The understanding of learners' culture, their everyday activities and experiences not only enables teachers to gain a greater understanding of their students, but also provides rich material to incorporate into classroom learning activities (STRINGER, CHRISTENSEN & BALDWIN, 2010).

It also provides an opportunity for teachers to understand their students in a richly meaningful way, and in the process, develop relationships that enable them to accomplish their work more effectively. In this framework, cultural artefacts and mathematical ideas embedded in it were the source domain, which mediates teaching and learning of the target domain, the abstract concepts of mathematics. The contextualization of school mathematics enables them to successfully accomplish the rewarding task of facilitating their students' learning.

5 Methods and Procedures

This study was intended to explore the ethnomathematical ideas embedded in cultural artefacts and their role in the teaching and learning of school mathematics. To answer my research questions, I resolutely situated myself as a qualitative researcher. Choosing the most appropriate methodology, that reflective process led me to select ethnography. I choose ethnography as the methodology because it looks at mathematical ideas in different cultural artefacts constructed by the group of people as a socio-cultural process (TAYLOR & BOGDAN, 1998). Ethnography can be a primary methodology for collecting empirical data from the field regarding the mathematical ideas, knowledge, and practices in different cultural artefacts.

I used ethnography to describe, interpret, and reveal the meaning of cultural activities regarding ethnomathematical ideas embedded in cultural artefacts and activities. While conducting this research, I continuously addressed the questions of interest involving mathematical ideas embedded in the process of constructing cultural artefacts and their ways of teaching and learning in their cultural settings. The implicit mathematical ideas used by the group of people in the process of performing their everyday job positioning myself to engage in the research techniques as described within an ethnographic paradigm.

To obtain the answer to my research questions, I purposively selected five people involving in different income generating cultural activities. The cultural artefacts regarding mathematical ideas embedded in the surrounding of the public secondary school of sample school were captured by using ethnographic tools. A total of five school mathematics teachers and 12 students from the school level were selected for the study. The data regarding the mathematical ideas embedded in different cultural artefacts were collected through observation and in-depth interviews with a group of people in a natural setting. Focused Group Discussion (FGD) of teachers and students were conducted separately in order to examine the contribution of cultural artefacts in the process of teaching and learning of mathematics. This was done with the help of interview guidelines and

observation checklist.

With regarding the data recording, the researcher chooses from several classical and contemporary positions and records the behavior and activities of the people in a natural setting through field notes (ANGROSINO & ROSENBERG, 2011). These field notes included paper-pencil, photographs, video or audio recorders with the consent permission of the research participants which can capture the lived experiences of the person or group within the context of the social setting. I carefully recorded all the possible conversations with the help of the video camera and took field notes as much as I could. I collected the data from multiple sources during the course of my study. I reviewed all of the data gathered from the multiple sources (CRESWELL, 2009) and then organized them into categories or themes that cut across all of the data sources. After observing the data, I linked them with many possible theories to interpret them.

I triangulated the data and the theoretical closures and gave meaning to my findings. In this process, I tried to produce accurate descriptions of the contents. Interpretation involved attaching meaning and significance to the analysis, explaining descriptive patterns, and looking for relationships and linkages among descriptive dimensions. In my study, the cultural artefacts and its associated practices in the students' community and their ways of understanding the natural phenomena, and their ethnomathematical knowledge embedded in it were analyzed with the notions of pluralism. In this study, the analysis of the research was validated and made more reliable by triangulating the statements among the research participants, their ways of presenting the text in the several times of data collection periods.

6 Metaphors for Teaching and Learning Mathematics

In this paper, I have discussed some cultural artefacts and practices associated with those artefacts that can be mediated for the development of mathematics ideas. One of my objectives was to explore the mathematical ideas embedded in cultural artefacts in the out-of-school environment. It was also intended to assess the contribution of cultural artefacts and associated practices in the process of teaching and learning of school mathematics. Cultural artefacts can be viewed as a series of mathematical ideas and concepts organized in an implicit manner. They practice their own mathematics within the cultural artefacts and activities associated with it. The emic knowledge of learners' community embedded in different cultural artefacts and practices exhibit a lot of ethnomathematical ideas.

The ethnomathematical ideas embedded in the familiar context of the learners' could be

the source domain for the teaching and learning of school mathematics. In my study, the familiar context of the learner that can be facilitated to understand abstract and different concepts is viewed as a source domain of conceptual metaphor. Thus, ethnomathematical ideas embedded in different cultural artefacts and practices associated with it are the source domain of the conceptual metaphor. My study argued that the conceptual metaphor is a powerful tool that assists to communicate the abstract mathematical ideas through familiar and meaningful objects. From the interaction with my research participants, there are a lot of informal mathematical ideas observed in the out-of-school environment.

The cultural artefacts observed in the surrounding of the out-of-school environment has a great potential to communicate school mathematical ideas. The ethnomathematical ideas embedded in cultural artefacts are effective metaphors to communicate the abstract concepts of school mathematics. I found that the teachers were using ethnomathematical ideas of different groups of people as a metaphor in the process of teaching and learning of school mathematics. In the following sections, I have discussed the ethnomathematical ideas practiced by different groups of people in their everyday activities and cultural artefacts constructed by those groups of people and their contribution to the process of teaching and learning of school mathematics.

6.1 Money and Teaching Place Value

Money is one of the cultural artefacts familiar to everyone from children to old aged people. It has a strong connection with all culture and it has been highly valued in this physical world. Everyone, even illiterate, recognizes the denominations of different currencies in terms of size, color, image, print, and texture. Nepalese currency and its denominations are probably unique since we find every denomination varied in terms of length, breadth, color and portrait in it. The most familiar denominations are one, five, ten, twenty, fifty, hundred, five hundred and thousand. Each has important cultural value and importance. Each note has its own definition as we can see in table 1.

Table 1: Nepalese Bank Note and its Features

Bank Note (Currency in Rs)	Portrait (Image in Note)	Color
1	Musk Deer	Dark Gray
10	Antelope	Gray
100	Rhinoceros	Green
1000	Elephant	Silver

Source: Author's personal file

In Nepal, whenever there is a talk about Rs 100, the imprinted image Rhino, and its green

color comes in mind or just vice-versa. Even it is common in conversations like when my son needs to ask for some money, he tells me “Pa, I need two *Hatti* (Elephant).” He was asking me for two thousand rupees (1USD = NRs.113.9, 15 aug. 2019). It might sound insane but it is a common interaction seen between people from a teen to the oldies. It is the same for other denominations. As a whole, we can easily understand 10 Musk Deer equaling to 1 Antelope, or 10 Rhinoceros equaling to 1 Elephant. This is equivalent to an understanding of 10 ones as 1 ten and 10 hundreds as 1 thousand. In the same way, 10 green notes equal 1 silver, which can equivalently be understood for 10 hundreds as 1 thousand.

In this regard, money can be a real-life example to teach different concepts in mathematics. Particularly this can be a powerful metaphor to conceptualize place value. During my survey, I asked some students if 2 or 8 had greater value in number 28, alas they replied that 8 was greater. The blunder they made was within the limit of my expectations, in fact, a chance for my research to experiment the efficiency of money as a metaphor. I took out the denominations of 2 tens, and 8 ones and asked them what was the total amount. They calculated them to be Rs. 28 in total. I again asked them whether 2 or 8 had a higher value. They finally answered the 2 had a higher value with a sight of realization. The use of money for developing the concept of place value can give it an actual significance.

The cultural artefacts can be used as a motivating stepping-stones to launch new mathematical knowledge (BONOTTO, 2007). He further explained that cultural artefacts offered the opportunity of making connections between mathematics incorporated in real-life situations and school mathematics. These artefacts are relevant to children; they are meaningful because they are part of their real-life experience, offering significance references to concrete situations. About the use of metaphors in teaching and learning of place value at the primary level, one of my research participant T₄ used a money metaphor to teach place value. As money is familiar to each student, its connection to the mathematical ideas of place value seems to be very fruitful. To teach the place value at primary grades, she used the note of rupee one to represent the one's units, the 10 rupees to represent the tens unit and the hundred rupees to represent the hundred of the unit.

I took a post-class interview with two teacher participants who used a money metaphor to teach the place value at primary grades seems to be satisfied and happy. The use of place value during the counting of numbers seemed to be really appealing with the positive response from both teachers and the students. They gained the value of each digit from the numbers. About the use of metaphors in teaching and learning of place value at the primary level, one of my teacher participant T₄ speaks:

After I joined the collaborative action research, I got wonderful ideas and opportunities to teach place value using money metaphors. As money is familiar to each student, its connection to the mathematical ideas of place value seems to be very fruitful. To teach the place value at primary grades, I used the note of 1 rupee to represent the ones units, the 10 rupees to represent the tens units and the hundred rupees to represent the hundreds units.

My other research participant agreed with the views of T₄. Further, T₅ speaks,

Money is a powerful metaphor as students seem to like talking about and playing with money. So I started using the money metaphor to teach the concepts of place value at the basic level of education. So I took the ones, 10 ones for a ten, 10 tens for a hundred and 10 hundred for a thousand and so on.

Realizing this view, it was found that the use of money metaphor to teach the concepts of place value at the basic level of education really made a difference in the learning process. From the observation of class, it was found that the concepts of ones, tens, hundreds, thousands through money mediated to conceptualize the ideas of place value for ones, 10 ones for a ten, 10 tens for a hundred and 10 hundred for a thousand and so on. The classroom activities of the teacher and the interaction supported the lines of Hutchens (2015) who viewed that the beauty of money with place value is that it gives place value a real meaning. Thus, it is concluded that money is a powerful metaphor to teach and learn one of the most important ideas of arithmetic because the concept of place value is very fundamental which helps to teach the mathematical operations of addition, subtraction, multiplication, and division.



Figure 2: Money with different Denominations as a Metaphor for Place Value (PRADHAN, 2019, p. 197)

The household ideas and knowledge, which students experience in their everyday activities in their familiar context provides the opportunities to learn school mathematics. The students' familiar context facilitates a systematic and powerful tool to represent the abstract concepts of mathematics. In this connection, I always advocate for Cummins (1996) "No learner is a blank slate" cited in Gonzalez, Moll and Amanti (2005, p. ix). It is believed that the students bring some sort of

mathematical ideas and knowledge into the classroom. The ideas and knowledge possessed by the children help to unlock difficult and abstract concepts of mathematics.

Mathematics lessons can be made interesting and effective from the students' point of view if it is relating to the real-life context of the students. If we relate a mathematics lesson to the real life of the students, the attitude of students towards mathematics is positive and student interest in learning of mathematics increases. Money is one of the real-life examples to teach different concepts of mathematics. It has a strong connection to all cultures and given high valued. Therefore, the concept of place value could be the linking metaphor for the teaching and learning of other concepts of arithmetic.

6.2 Money and Conceptualizing Integers

The concept of integers is introduced at grade VI in the school mathematics curriculum. It is a very important part of the curriculum and it symbolizes a move from concrete to abstract thinking. Even the secondary level students have misconceptions in tackling the problems regarding the negative integers. When I asked to identify the greater number in -5 and -8, most of the seventh-grade students have an incorrect answer. For making the concept of integers more easily understandable, there can be the use of many metaphors, which are familiar to the students' out-of-school context. However, it becomes a difficult task for the teacher to figure out which metaphor would suit best to teach contents in the classroom teaching with good conceptual understanding.

When analyzing discussion during a workshop in a teacher support program in my sample school, different metaphors were proposed for the teaching and learning of integers. One of my research participants gave the MONEY is INTEGER as a metaphor to conceptualize integers. Many researches have been done in the area of integers about how can students of basic level be conceptualized with the notion of negative integers thereby students developed conceptual understanding in the subject. While teachers are going to deliver new abstract mathematical concepts, the metaphors are the effective tools to communicate the concepts. However, mathematics teachers are not always aware of the metaphors they use (FONT, BOLITE & ACEVEDO, 2010).

In the classroom observation of one of my research participants, I found that the teacher used several metaphors in the process of teaching the concept integers. But she was unaware of the question of what type of metaphor did she use. Most of the teachers used metaphors without

noticing it as if they were the metaphors. I analyzed that the metaphors used by T₃ in her study of teaching integers at grade six was MONEY is INTEGER metaphor. She told me that she generally used some familiar examples that students encounter in their everyday lives.

Table 2: Integers is Money Metaphor

Source Domain	Target Domain
Neither loose nor won money	Zero
You won Money	Positive Integer
You lose Money	Negative Integer

Source: Pradhan (2019, p. 233)

Teachers use money metaphor as the basis of integer that was compared with having or not having the money. The winning of money signified positive integers, the loss of money signified negative integers and the situation of neither a loss nor gain signified zero. The feeling of win, lose and neither win nor lose are well-known to every student of this age group which can act as the source domain to understand abstract concepts of positive, negative and zero integers. Therefore, money, a cultural artefact, could be the grounding metaphor for the teaching and learning of integers.

Money, as a metaphor, can be used as a very effective tool in the teaching of integers as it holds a great impact in this physical world. There is probably no child who lags the idea of earning and spending money. One of my teacher participant T₅ speaks:

Students have a misconception about the negative integers. Even a number of seventh graders have no clear ideas about the identification of larger and smaller negative integers, say -10 and -3. In my class on integers, I always give the example of assets and liabilities to conceptualize the content. People who have more liabilities are considered as small negative numbers and vice versa. For example, people are less poor who have to pay a small amount than the people who have to pay more amount. Therefore, -10 is smaller than the number -3.

The assets and liabilities can also be the metaphor for the understanding of positive and negative integers. Assets add positive income each period and liabilities (debt) require payment to service it. From the interview with students and teachers, I found that the money metaphor was equally significant in the course of teaching integers. The metaphors ASSETS is POSITIVE INTEGER and LIABILITIES is NEGATIVE INTEGERS used by teacher participant T₅ have been a powerful metaphor to conceptualize the integers. As per my observation of the T₅ class about integers, I found the connection of money with the teaching of integers very graceful. She had connected the earning, spending and owing of money directly with concepts of integers. The students' participation in the task, their facial expression during the classroom teaching was

entertaining and happy. They actively participated in classroom activities. The students' familiar out-of-school context and their experiences and practices enhance to understand the concept easily.

6.3 Clock Metaphor for Conceptualizing Rounding off Numbers

Rounding off numbers is an important skill in every sector of human lives in general and particular in mathematics. Estimation of skill gives an idea about possible answers without doing a lot of work. This skill allows us to estimate numbers and make them easier to understand. Rounding off numbers to the nearest multiple of 10, 100, 1000, or million has great significance. In Nepal, the Central Bureau of Statistics (CBS) conducted a widespread national census in 2011. The CBS determined that the population of the country was 26,494,504. That number is hard to remember and if we say the population of Nepal is 30 million it is a good estimation because it doesn't make any real difference with what the exact number is.

In daily life, estimation is great for giving intelligent guesses about the possible amounts. The rounding of numbers in the nearest ten, hundred and thousand are introduced in the mathematics curriculum at the basic level of education. There are different metaphors to communicate the abstract concepts of rounding off numbers. The common metaphors used in the discussion of the contents were clock metaphor, number line metaphor, path, and fictive motion metaphor. In this paper, the clock metaphor is put forward to teach the concept of rounding off numbers.

The concept of rounding off numbers is used in everyday activities and basically used to describe the situations like morning, day and night. Any nonprofessional can also usually conceptualize the time in these three states of time. We eventually say that its morning, it's already a day and its night and so on. Which time is belonging to the morning, day and night? That is not a great deal here. The important thing is that our everyday interaction involves the rounding-off the time like morning, day and night. Anyone who says, its morning! It is not difficult to understand that he is rounding the interval of time in the morning.

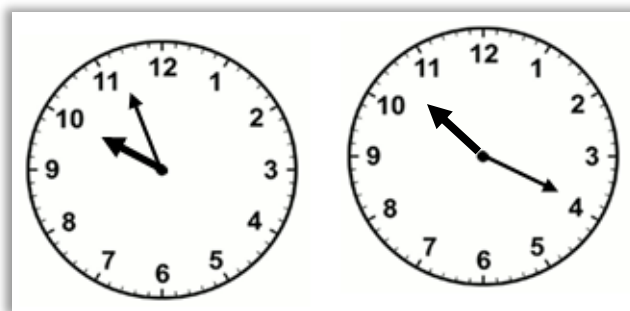


Figure 3: Analogue Watch as a Metaphor for Rounding-off Numbers (Author's personal file)

If we ask a person with a watch about what time is it in the clock, then the person probably answers the time to be 10 o'clock even when the exact time in the clock would have been 10:03 or 9:56 or any nearest digits. This is because; people divide an hour into four-fifteen minutes viz. an hour, quarter past, half past and quarter to-. The concept of rounding of time is common in everyday interaction of the group of people. Even when the exact time is 10:57, the time is told to be 11 o'clock or even when it is 10:19, the time is told to be quarter past 10 which is equivalent to 10:15. The minute here is rounded off to its nearest one-fourth of a complete rotation. Thus, the watch can be a grounding metaphor for the teaching and learning of the concept "Rounding off Numbers" inside the classroom. We can conceptualize the concept for the rounding off numbers implicitly in course of viewing the time in an analogue watch.

6.4 Mat and Embedded Mathematical Ideas

Weaving is one of the common cultural activities practiced in different communities in Nepal. The weaving of textiles, sitting mat, sleeping mat, basket, and other stuff reflects the cultural values and identities. Various mathematical ideas and thinking are inherited in the process of construction of the mat. Indigenous people have implicit mathematical knowledge with the ability to perform a task but without the ability to explain their deeds (PRADHAN, 2017). This implicit mathematical knowledge is embedded tacitly in their activities. Mosimege and Lebeta (2000) also reported that indigenous people use different mathematical concepts like estimation, tessellations, and symmetry in the construction of traditional artifacts and in various other cultural activities. I observed that the mat weavers exhibited sophisticated geometrical ideas in the process of construction of a net of the mat. The knowledge they practiced in the process of construction of a net of the sleeping mat used the theorems of Euclidean geometry implicitly.

Mat weavers practice mathematical ideas and knowledge implicitly in the process of construction of mat. They use sophisticated geometrical ideas while constructing rectangular

frames. Two poles are fixed in accordance with the length of mat required and the third pole is adjusted as per the breadth of the mat. To adjust the fourth pole, they use the X-test that is the process of constructing the frame of the mat involving tacit geometrical ideas that two diagonals of a rectangle are equal in length. In a cultural village of Nepal, a rectangular form of sitting or sleeping mat may be rolled up when it is not in use. Some people use sleeping mats to larder for the purpose of reserve paddy. It then takes approximately the form of a cylinder. From the observation of the situations, this cultural experience provides an opportunity for students to obtain an idea of calculation of the curved surface area, the total surface area and the volume of a cylinder.

The finished product is analysed to assess the embedded mathematical ideas in the mat and other cultural artefacts. We have a mat ABCD of length L and breadth H. Let us transform the mat ABCD into a cylinder by rolling up such that AC and BD are just in contact.

Here, Area of initial mat ABCD = Surface area of the cylinder = L. H
 It is evident that the circumference of the base of cylinder (C) = L
 This implies that $2 \pi R = L$ gives $R = \frac{L}{2\pi}$
 Let A be the area of the cross-section area of the circular cylinder, $A = \pi \left(\frac{L}{2\pi}\right)^2$
 Also $V = A \times H = \frac{L^2}{4\pi} \times H = \left(\frac{L}{2\pi}\right)^2 \pi \cdot H$. It gives, $V = \pi R^2 H$

From the observation of the situations, this cultural experience provides an opportunity for students to obtain the idea of calculation of the volume of a cylinder and the study of different geometrical properties inherited in it. It is argued that it is possible to use indigenous mat weaving as a metaphor for the teaching and learning of mathematics at different levels of education.

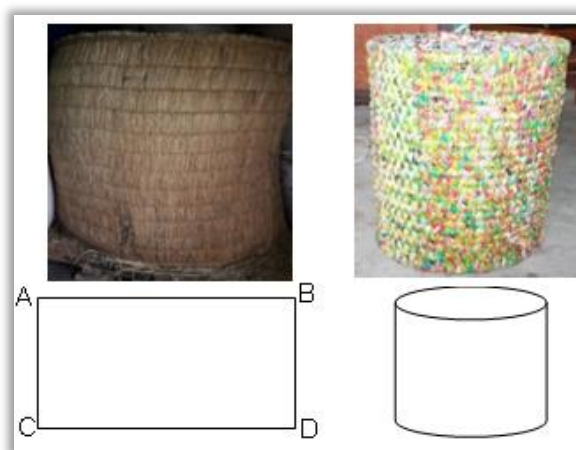


Figure 4: Folding a mat: a model for cylinder (PRADHAN, 2019, 136)

The incorporation of weaving activities in the process of teaching and learning enhance mathematical understanding of the students. The teacher, in his classroom, connected this concept

by measuring the dimensions of the mat and rolling it to conceptualize the concepts of curved surface area, total surface area and volume of the cylinder formed. Then I took a post-class interview with the students. I asked the students about how they felt about the teaching with activity-based pedagogy. Regarding the effectiveness of introducing cultural activities in the mathematics classroom, one of the student participant S_1 viewed

I have learned most of the mathematical concepts through rote and memorization just with an aim to solve problems and score good marks without any level of understanding. Now, the abstract concepts and ideas of curved surface area, total surface area and volume of a cylinder were visualized easily through these activities.

From the interaction of my student participants, I came to know that, the students' everyday activities and experience play a vital role in the development of mathematical concepts. One of the students S_2 replied

Before the use of this teaching model, we were just made to memorize the formula for the purpose of solving common problems. Later, when this model was taken in action for teaching, we could easily visualize the abstract concepts and visualize it as a mathematical object.

Another student S_3 viewed

After this class, I was surprised to know that mathematics could even be linked with the cultural activities that we were performing just for household jobs. Now, I think that everything that we study can be linked with cultural activities making even these boring classes interesting. This lecture really proves it.

The use of cultural artefacts and everyday activities of learners in classroom teaching seems to be really appealing and the outcome of the understanding as per the students was quite appreciable. The use of ethnomathematical practices of mat weavers as a pedagogical tool shows the importance of the contextualization of problems (ROSA & OREY, 2012). Mathematical thinking and methods are quite different in various cultures (GERDES, 2001). The mathematical ideas hidden in the process of constructing the frame to weave a mat in the rural community in Nepal is mostly equivalent to the methods that the Mozambican peasantry used for constructing rectangular bases of houses (GERDES, 1999). Further, Gerdes (1997) explored that the construction techniques of the housebuilders facilitate to formulate the rectangle axiom. From the observation of the different processes of mat weaving, it was found that it includes a lot of mathematical ideas, implicitly and tacitly embedded in it.

6.5 Carving and Exploration of Geometry

The notion of symmetry has an important role in the development of mathematical concepts and science. In everyday life, the most common case of symmetry is associated with a mirror reflection. In this vein, Capra (1975) defines a symmetric figure as that which one can draw a line through it and thereby divide the figure into two parts which are exact mirror images of each other. By understanding the role of symmetry in the visual recognition process, we can better recognize its frequency throughout a number of cultural domains. The mirror symmetry, or bilateral symmetry, is the symmetry with respect to reflection. A figure, which is indistinguishable from its mirror image, is called mirror symmetric. A way to think about this symmetry is to fold the image in the middle and check if the two halves are identical (SPARAVIGNA, 2000). The rotational symmetry is different because it is quite natural for us to follow the image in its rotation in the space. This symmetry produces a feeling of motion and evolution. A breaking of symmetry, in this case, enhances the idea of interpenetration or contrast.

One of my research participants Biru (Pseudo name), who carve stone, said that “people love to buy the item if it looks attractive. So my effort is to make an image in the stuff more beautiful”. The image will be more beautiful, and eye-pleasing if the images are symmetric in the pattern. It exists not only in art and design, but it also exerts its strong presence in mathematics, in the physical world of science, in history, and even in story plots and character development. They construct different geometrical patterns in their works. They use rectangular coordinate axes while start to draw a pattern. The symmetries are found in their activities.

Every beautiful thing in the world possess mathematical properties, and the images possess the golden ratio. From the observation of the workplace of the carver, it was found that the coordinate axes, symmetry, reflection are the mathematical ideas embedded in their drawing a pattern. The stone they bring to make different stuff was more likely to rectangular form. I asked him “why do you make the stuff in circular shape even though it is difficult and time-consuming?” Regarding the answer to this, Biru says that the image that he carved possess mathematical properties of symmetry tacitly in order to make the stuff more beautiful and fascinating. He further said that the circular object seems to be more fascinating rather than of rectangular form. In this regard, a circle is a perfect geometrical figure than the rectangle and/ or square because the circle has an infinite number of symmetry axes (FRANCOIS, 2019). The carver had implicit and tacit knowledge of symmetry that helps to make the images more beautiful and eye-pleasing. They construct different geometrical patterns and designs in their works.

In the village of Nepal, symmetrical images are painted on either wall of the door in a house.

The wonderful mathematical ideas and concepts which are practiced in the construction of different patterns in stone carving. The stone carver uses the emic view of the mathematical knowledge in the process. The mathematical knowledge they practiced since long complimented to their everyday lives and developed across generations verbally. So, it is impossible for a researcher to go through the emic approach because they all have preconceived perspectives, ideas, and theories. In this regard, Fetterman (2010) viewed that “most ethnographers start collecting data from the emic perspective and then try to make sense of what they have collected in terms of both the native’s view and their own scientific analysis” (p. 22).

This implicit mathematical knowledge is embedded in their activities tacitly. Mosimege and Lebeta (2000) also reported that indigenous people use different mathematical concepts like estimation, and tessellations, and symmetry in the construction of the traditions artefacts and cultural activities. The stone carver uses a lot of mathematical concepts and knowledge. This knowledge is sufficient for performance that is consistent with rules, even though the person might not be aware of the rules. The field data also supported the findings of Millroy (1992) that the stone carver uses tacit mathematical knowledge in the process of constructing different stuffs as Millroy (1992) observed that the carpenters’ physical act of designing and building furniture involved tacit mathematical knowledge. In this situation, they practice the mathematical ideas of the circular shape, center, and radius of the circle; the coordinate axes, reflection and symmetry of different geometric patterns.



Figure 5: Stone carving: different forms of symmetry (PRADHAN, 2019, p. 143, 159)

The indigenous language pattern of the speakers reflects mathematical concepts and ideas (OWENS, 2012) who observed how the most indigenous languages of Papua New Guinea (PNG) possess mathematical concepts like volume, mass, area, and length. The children from indigenous communities are deeply immersed in their own cultural world. Their home language reflects the mathematical thinking of the people in own ways (BARTON, 2008; OWENS, 2012) and I also observed that stone carver have tacit mathematical knowledge of circle, identification of center, diameter in the various stage of construction of geometrical pattern and in their conversation. Stone

carver use circle in designing the different pattern in the stone.

The circular pattern helps them to make a pattern in symmetrical form. Symmetry in its various forms was found in the designs on the arts and artifacts constructed in a different community of Nepal. Rosa and Orey (2006) viewed that one of the major objectives of the ethnomathematical research is to look for possibilities of incorporating the mathematical ideas embedded into the cultural context of students and teachers for improving the teaching and learning of school mathematics. There is a prevalence of symmetry in designing textiles, sand painting, wall painting, pottery, arts, and artifacts of the people in different cultures.

6.6 Bell and Exploration of Geometry

Nepal is a secular country. The main religion of Nepali is Hindu. They worship *Brahma*, *Bishnu*, and *Maheshwar* and they are taken as the *Trimurti* (Three God) in Sanskrit. The three forms are the supreme divinity in Hinduism. They are considered as the cosmic functions of creation, maintenance, and destruction. Particularly, they are leveled as *Brahma* the creator, *Bishnu* the preserver, and *Maheshwar* the destroyer or regenerator. Hindu people often visit temples to worship god and goddess. We did encounter the bells to enchant the prayers and to symbolize the presence of the devotee in the temple to worship the god. The term geometry may be evolved as a tool to measure the land. It is thus known as a measurement of “Geo”. However, our school geometry really does not measure the associated problem regarding the measurement of the distance between different two places. It is also insufficient to measure the land area of different landscapes. Thus, Euclidean geometry is the geometry of plane.



Figure 6: Bell and Exploration of Geometrical Ideas (PRADHAN, 2019, p. 149)

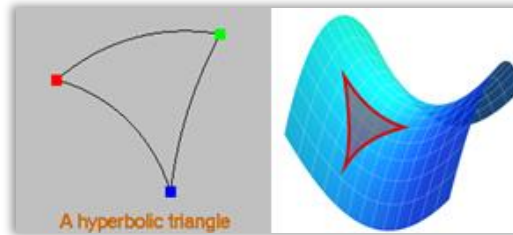


Figure 7: Hyperbolic Surface (PRADHAN, 2019, p. 149)

The mathematics teaching and learning would be more interesting and effective if the appropriate connection is made between out-of-school contexts to the school mathematics. The study of cultural artefacts and ethnomathematical ideas embedded in it are the sources for teaching and learning of school mathematics. Ultimately, I decided prehistoric *Guheshwori* temple as the study location for the field visit with the aim to connect cultural artefacts as the metaphor for teaching-learning mathematics. After reaching the field place, all the students were requested to observe the temple and its surroundings and note down the geometrical objects and the probable mathematical concept that they could identify.

After some time of observation, each group was requested to present their observations and findings. Each group involved in the common task serially presented their findings. The common observation made by the students were the 2D shaped objects like triangle, square, quadrilateral, circle, oval, octagon, trapezium, parallelogram and rectangle. They also observed 3D shapes like hemisphere, cone, frustum, sphere, cube, cuboid, cylinder, prism and pyramid. They sorted out the concepts of concentric circles, transformation, reflection, rotation, symmetry, pattern, and tessellations.

One of the objects they encountered was bell and they were unaware of the surface of it. In this vein, while observing the temple bell, it is possible to describe the distinctive features of hyperbolic geometry and was the metaphor to contextualized the notion of it. The different types of triangles can be drawn on the surface of the bell. It is considered that the inclusion of ethnomathematical ideas in school mathematics valued students' cultural backgrounds and experiences. The observation of different cultural artefacts in the surrounding of the temple would motivate students to take mathematics relevant to their lives outside the classroom.

From the above hyperbolic triangle, it is seen that the sum of the angles of a triangle is always less than 180 degrees, which contradicts the notion that the sum of the angles of the triangle in Euclidean plane is always equal to 180 degrees. Bell is one of the interesting artefacts that have many properties of non-Euclidean geometry. The various property of hyperbolic geometry can be found in the bell. The parallel lines meet at a point, the sum of the internal angles of a quadrilateral

is less than 360 degree and other related properties also can be found from the observation of bell. To distinguish the different types of planes, we would like to draw three different planes which may be helpful to generalise the different types of geometrical figures of Euclidean plane, Hyperbolic plane (surface) and Elliptic plane (surface). The bell can be described metaphorically as a bell-shaped curve to normal distribution. The bell was found to be an effective tool to conceptualize the notion of hyperbolic geometry at a higher level than a basic level.

6.7 Rangauli Mandala and Geometrical Pattern

Nepal has rich cultural traditions and peculiar rituals. *Rangauli* mandala is constructed on the occasion of *Dipawali*. It is drawn using the rice flour including seven different colors and seen on the floors of buildings and in front of the worship room during the festival. This drawing requires different geometrical patterns and spatial reasoning (PRADHAN, 2018). The number of concentric circles, the number of symmetries both bilateral and rotational are found in the *Rangauli* mandala. Different colorings are also associated with this drawing. Regarding the construction of *Rangauli* mandala, I asked one of my research participants Sushila (Pseudo name), how is the mandala pattern drawn. She replies that the:

(...) mental image of the pattern helps to draw a *Rangauli* mandala. The cognitive map of the mandala is important thing for that. We start from a point and draw some concentric circles. Anyone can draw any shapes inside the regions in concentric circles. Some may draw an eight-pointed star or eight petals of a lotus as per their choices.

From the interview with Sushila, I came to know that the construction of mandala is a mental construction. The different geometrical pattern found in their construction is largely hidden from the participants. And the ways of drawing of such cultural arts and artefacts are craft model approach. Image 6 is the mandala constructed by Sushila herself in front of the main doorways of the house. I asked her how did she draw the eight-pointed star. She had already completed drawing the mandala.



Figure 8: *Rangauli* Mandala (PRADHAN, 2018, p. 337)

After my intense request, she chose to sketch it out as shown in Figure 3. The process of her drawing was that first, she drew concentric circles and divided the smaller circle into four equal parts by drawing two mutually perpendicular diameters. Then she further divided each part into two more halves forming eight parted circle. Finally, she retraced the consecutive lines by making them converge at the circumference of the larger concentric circle forming pointed triangles.

From the observation of her sketch of an eight-pointed star, I have come to know that they are practicing sophisticated mathematical ideas in the process of constructing mandala. The *Asta Matrika* or eight-pointed star has great significance and has religious meaning in Hindu culture. Every creation and perception of the pattern has a logical as well as aesthetic component (ASCHER, 1991). The *Rangauli* drawing involves complex mathematical activity and a strategic understanding of spatial reasoning. It is important to explore the hidden mathematical ideas in the process of constructing such cultural artefacts. For that, I have conducted interviews with some other people who are constructing such artefacts as their cultural tradition. In this regard, I asked another research participant Kamala (Pseudo name) about the knowledge they learned to construct such beautiful artefacts and her mathematical ideas associated with it. She replies:

I learned to make this artefact by observing the ways of drawings of my mother as in the same of how these children observing patiently to my activities here. First I draw a sitting place for goddess *Laxmi* at the center as we are going to worship the goddess. Then I drew some larger circle and eight petals of lotus as we believe that she likes to lie over the pleasant lotus flower.

Rangauli is a symbol of good fortune. Rice flour used for *Rangauli* drawings provides nourishments for smaller animals, such as birds and ants. This is a symbolic act of showing the necessity of sharing and maintaining proper relationships with others. It also reinforces the respect for nature and relationships with other human beings and animals. Hindu women almost exclusively practice this form of art. *Rangauli* is being constructed as cultural product from generation to generation in a process of craft model learning approach. It is consistent and perfection in their drawings of the mandala. Though they lack formal education, they possess sophisticated mathematical ideas in mandala construction. From the observation and interview with them, I have come to know that the indigenous people have had their own mathematical ideas and thinking in order to perform their everyday job.

Teaching mathematics becomes more interesting if the contents are related to the students' familiar environments. Students' everyday interaction with the cultural environment provides more opportunities to interact and conceptualise mathematical ideas. The cultural

activities and artefacts of the students involve a lot of mathematical knowledge and ideas. These mathematical ideas embedded in the students' cultural environment, which is familiar to the students, provide a good environment to learn. This environment acts as an important tool to communicate mathematical ideas.

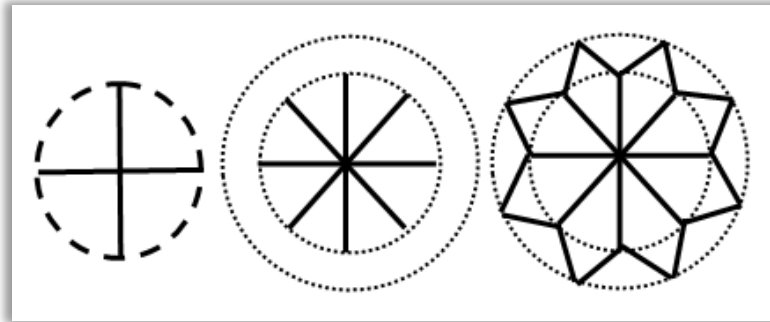


Figure 9: Process for Construction of Mandala (PRADHAN, 2018, p. 338)

The elders, generally female personals, blissfully draw out the celebratory artefact, the *Rangauli*, where they pour their intense ideas and creativity in it. In addition, for any creation to look striking there is the definite use of mathematical ideas either implicitly or explicitly. In this view, I interacted with some students regarding their experiences with the *Rangauli* construction with their elders. To this note, my student participants speak:

One of the reasons for me to like *Dipawali* is that my mother and sister draw the *Rangauli* and even I can put in some colors in it. I get so fascinated to make use of so many colors and the final art always looks so beautiful that I can just see and mesmerize its beauty for hours.

Looking at her excitement it was sure that the connection of such out-of-school ideas inside the classroom could develop a positive attitude towards the subject, which definitely boosts the understanding of the mathematical concepts. Another participant added, "I patiently observed my mother's work when it's about the *Rangauli*. At the start, she sketched the pattern of the mandala. Then she carved it to a beautiful object by filling it with different shapes and colors in it." I asked them to sketch the pattern of the mandala from their memory. I observed the same perfection of the outline in their workbook. I asked them if they could see any sort of mathematics in it, a student answered after an unusual pause that there were some shapes like circle, curves and lines.

From the observation of students' workbook and interaction with them, I came to know that they are performing their cultural activities rather than doing some mathematical tasks. However, there are many mathematical ideas embedded in their construction. The main problem for easy understanding of concepts is that there is a lack of connection between the two mathematical worlds- school mathematics and cultural mathematics. The mathematical ideas practiced in

students' environmental context may be used as a (cultural) metaphor for the teaching and learning of school mathematics. The informal mathematical ideas and knowledge practiced and used in everyday activities are the sources domain for the understanding of abstract mathematical ideas. Thus, the ethnomathematical system of the cultural group can enable a better understanding of school mathematics.

7 Possibilities of Incorporation of Cultural Artefacts in Mathematics Teaching

Teaching mathematics becomes more interesting if the contents are related to the students' familiar environments and ethnomathematical ideas they practice in the out-of-school context. Students' everyday interaction with the cultural environment provides more opportunities to interact and conceptualise mathematical ideas. They construct mathematical knowledge with the help of their prior knowledge, experience, active participation in their environmental activities and cultural artefacts surrounding them. The household activities of the children and cultural artefacts involved many implicit mathematical ideas. However, our school mathematics curriculum and teacher training is largely ignoring the learners' cultural activities and their ethnomathematical ideas (PRADHAN, 2017; EZEIF, 2002).

Rosa and Gavarrete (2017) also viewed that children's ethnomathematical knowledge and learning approaches are not taken into consideration in the formal school mathematics curricula. The mathematical ideas from the group of working-class people culture, the acknowledgment of their ways of knowledge generation and transmission, and students' experiences should be blended with formal mathematics in the classrooms (PRADHAN, 2017). The mathematical ideas embedded in the students' cultural environment, which is familiar to the students, provide a good environment to learn. This type of environment/ context provides a good opportunity for students to explore and communicate mathematical ideas.

Mathematical ideas and thinking are embedded in every environmental activity of a group of people. However, the mathematical ideas they possess in order to perform their everyday job remains largely hidden for them. Mathematical anthropology uses mathematical modeling in historic, ethnographic, and material culture studies to describe the material and cognitive patterns of a certain group of people (EGLASH, 2001). In this vein, Rosa and Orey (2010) viewed that mathematical modeling is a methodological tool that may be used in the ethnomathematical program. Ethnomathematics can reshape our greater cultural identity in a positive way by requiring the inclusion of a greater representation of the true mathematical practices and problems for a

students' own community (D'AMBROSIO, 1998; ZASLAVSKY, 1996). Symmetry in designing textiles, sand painting, wall painting, pottery, arts, and artefacts is prevalent in the people of different cultures around the world.

The mathematical ideas practiced in students' environmental context may be used as a cultural metaphor for the teaching and learning of school mathematics. The informal mathematical ideas and knowledge practiced and used in the day-to-day activities are the source domain for the understanding of abstract mathematical ideas. Thus, the ethnomathematical system of the cultural group can enable a better understanding of school mathematics. Regarding the possibilities of incorporation of cultural artefacts for the teaching of school mathematics, one of my research participants T₁ says:

I believe that mathematics is evolved from the culture. The different groups of people are using mathematical ideas implicitly in their profession. Their children are also doing the same work what their parents do. Children are also using same kind of mathematics. But the real problem is to connect their mathematics to school mathematics.

Most of the research participants reported that mathematics originated from the cultural activities of different society, from different racial groups around the world. Different professional groups of people are using mathematical concepts and ideas in their own ways. My data in the construction of different cultural artefacts claim the embeddedness of hidden mathematical ideas on it. Their implicit mathematics knowledge of the group of people provides an opportunity for their children to learn mathematics in the classroom. Our school pedagogy has given much importance to rote learning and it is not converged with the ways of knowledge generation and distribution of the local people (PRADHAN, 2017). Thus, I observed that the pedagogy we adopt in school does not acknowledge the out-of-school knowledge of the students.

However, the pedagogy used in out-of-school context was the craft model approach, which is common to the knowledge generation and distribution. This involves participatory and cooperative approaches in which they learn with the help of their parents as Vygotsky (1978) sees learning as an activity in which shared mathematical meanings are constructed socially. Thus, the mathematical ideas embedded in the out-of-school context and the pedagogy they use could be powerful metaphors for the teaching and learning of school mathematics. Teachers who have children's cultural backgrounds and funds of knowledge can link in the classroom.

Other research participant T₃ opined that "We teachers do not have time to think about to make mathematics teaching more culture friendly because of the overloaded curricula and over

duties in classroom teaching”. Connecting with the same question, other research participant T₂ questioned, “How can teachers think their lesson more culture friendly if they do not have sufficient time to manage?” But, another participant T₄ gives serious limitations of the teachers to make their class more culture friendly.

Time is not a problem at all to use cultural artefacts in the teaching and learning of school mathematics. Attitude and knowledge of the teachers about the cultural artefacts for teaching school mathematics are more problematic. But the problem is the lack of ideas on the selection of cultural artefacts for the teaching of the particular content of school mathematics.

They believe that incorporation of culture friendly pedagogy needs more time and extra effort to classroom teaching. Regarding the use of cultural metaphors for the teaching of school mathematics, my research participant T₂ opined that:

The use of cultural artefacts in mathematics teaching is evident. But we are unable to use it in our classroom teaching. How can a teacher who have the responsibility of taking five to six periods in a day can manage their own class from culture friendly pedagogy? How to prepare class with the view of cultural friendly pedagogy for certain mathematical content? If a teacher has one or two periods of responsibility, then s/he can think about which cultural metaphor fitted most appropriately.

Most of my research participants agreed with the view of T₂. They all accept the importance of cultural artefacts for the conceptual understanding of the mathematical concepts. The incorporation of cultural artefacts in the process of teaching and learning of mathematics enhances mathematical understanding to the students. From the interaction of my research participants, it was found that there are a lot of informal mathematical ideas present in the construction of different cultural artefacts. Those mathematical ideas are effective metaphors to develop spatial reasoning and communicate the abstract mathematical a. I found that the teachers were using ethnomathematical ideas of different groups of people as a metaphor in the process of teaching and learning of classroom teaching.

Teachers are the main agents to deliver formal mathematical content knowledge to their students. Their attitudes, beliefs and values determine how classroom teachers demonstrate alignment for the most effective and meaningful teaching practice (BEARDEN, 2012). Regarding the role of cultural metaphor in the teaching of school mathematics, one of my research participant T₁ viewed the cultural metaphor as a powerful tool for the development of mathematical concepts. Most of the participants viewed that the culture friendly pedagogy and the funds of knowledge for teaching and learning of school mathematics are effective for teaching mathematics. Almost all of my research participants agreed that cultural artefacts are potentially a very powerful tool for

teaching-learning of the mathematical concepts. The incorporation of metaphor in the process of teaching and learning of mathematics enhances mathematical understanding of the students and eases to transfer abstract mathematical ideas.

8 Concluding Remarks

Metaphors are common to everyone in their everyday communication. Even a child uses metaphors in their gameplay without noticing it. Metaphor is one of the powerful mediated tools that give a real meaning of objects in view of observers. In my study, the ethnomathematical ideas that are practiced in everyday activities of different groups of people, the mathematics embedded in different arts and artifacts in the out-of-school environment, the cultural games, and gestural activities that contributed to conceptualizing the abstract mathematical ideas were considered as metaphors. The culturally relevant pedagogy bridges students' home culture with school culture in the process of teaching and learning of mathematics. The people outside the classroom use sophisticated mathematical ideas to perform their everyday activities. For example, a mason uses the 3-4-5 method to construct the rectangular shape. Mat weavers use implicit knowledge of Euclidean geometry while they construct the frame for the mat.

Their indigenous knowledge and skills are sufficient for maintain their living. The ideas of estimation and approximation are fundamental and critical in the development of mathematical concepts. The major characteristics of home mathematics are estimation and approximation. The measuring system of the carpenter, estimation of Chundara in the process of constructing wooden stuffs, the ratio of different ingredients in the preparation of tea and the different mathematical ideas embedded in the kitchen involves the estimation and approximation. The mat weavers, textile weavers, stone carvers, wood carvers, small-scale businessperson and different groups of people possess highly sophisticated mathematical ideas in their everyday activities.

The people in the out-of-school environmental context use mathematical ideas implicitly for long. Their mathematical ideas and knowledge have practical validity but are neither acknowledged nor utilized in the school mathematics curriculum. In my study, different cultural activities and cultural artifacts provide an opportunity to explore the mathematical ideas embedded in the cultural context and help to connect school mathematics. The ethnomathematical ideas embedded in everyday activities of different groups of people can also be linked while teaching in the classroom to make it lively. Further, culturally relevant pedagogy builds on students' home culture as a means to foster success in the learning of school mathematics.

The students' out-of-school culture and embedded ethnomathematical ideas help to learn school mathematics. From the interaction to teachers and students, it was concluded that the cultural artefacts as metaphors substantially contribute to the process of teaching and learning of mathematics. For instance, the money metaphor contributes to teaching and learning of place value and to conceptualize integers; clock metaphor help to understand rounding off numbers; weaving mat, stone and woodcarving and other cultural activities facilitate understanding various mathematical concepts. This enabled me to conclude that the teachers need to figure out the cultural artefacts as metaphors and use them to teach and help students learn abstract concepts of mathematics. Most of the participants viewed that the culture friendly pedagogy for teaching and learning of school mathematics is effective for teaching mathematics. They agreed that the use of cultural artefacts and its incorporation in classroom teaching creates a positive attitude towards mathematics. They themselves enjoyed the approach of teaching and learning through the use of cultural artefacts and culture friendly pedagogy in the process of teaching and learning of school mathematics.

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